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Recommendation for Block Cipher Modes of Operation: Three Variants of Ciphertext Stealing for CBC Mode

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C O M P U T E R S E C U R I T Y

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Computer Security Division Information Technology Laboratory National Institute of Standards and Technology Gaithersburg, MD 20899-8930

June 2010



U.S. Department of Commerce

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Addendum
National Institute of Standards and Technology Special Publication 800-38A
12 pages (June 2010)
CODEN: NSPUE2

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1 Introduction

A limitation to Cipher Block Chaining (CBC) mode, as specified in NIST SP 800-38A, Ref. [1], is that the plaintext input must consist of a sequence of blocks. (In the rest of this publication, a block is called a "complete block" to emphasize the contrast with a "partial block" whose bit length is smaller than the block size.) Although Appendix A of Ref. [1] describes how padding methods can be used to meet this requirement, in such cases, the length of the resulting ciphertext expands over the length of the unpadded plaintext by the number of padding bits.

This addendum to Ref. [1] specifies three variants of CBC mode that accept any plaintext input whose bit length is greater than or equal to the block size, whether or not the length is a multiple of the block size. Unlike the padding methods discussed in Ref. [1], these variants avoid ciphertext expansion.

These variants are denoted CBC-CS1, CBC-CS2, and CBC-CS3, where "CS" indicates "ciphertext stealing," because when padding bits are needed in these variants, they are taken from the penultimate ciphertext block. The variants differ only in the ordering of the ciphertext bits. CBC-CS1 was specified as a suggestion on the NIST Computer Security Resource Center web site. CBC-CS2 is specified, for example, in Ref. [3]. CBC-CS3 is the variant specified for Kerberos 5 in Ref. [2].

Below are the specifications for encryption and decryption using CBC-CS1, CBC-CS2, and CBC-CS3, building on the specification of the CBC encryption and decryption in Ref. [1]. Diagrams are given for CBC-CS1 encryption and decryption. Each variant inherits the relevant requirements of Ref. [1], e.g., on the underlying block cipher, the key, and the initialization vector.

The following notational conventions apply to the specifications below:

- Bit strings are denoted with upper case letters; integers with lower case letters.
- The block size of the underlying block cipher is denoted b.
- For a bit string X, the bit length of X is denoted len(X).
- For a bit string X and a positive integer r that does not exceed len(X), the string consisting of the leftmost r bits of X is denoted $MSB_r(X)$, and the string consisting of the rightmost r bits of X is denoted $LSB_r(X)$.
- For an input block B and key K, the output block of the cipher function ("encryption") is denoted CIPH $_K(B)$, and the output block of the inverse cipher function ("decryption") is denoted CIPH $_K(B)$.

In principle, the input strings to encryption and decryption for each of the variants may be any string whose length is not less than b bits, but typically an implementation is designed to accept a restricted set of lengths. For example, the set of lengths may be

restricted to multiples of 8, so that the input strings may be represented with bytes/octets. The input lengths that an implementation allows are called the *valid* lengths.

Specification of CBC-CS1

Algorithm: CBC-CS1-Encrypt

plaintext P, such that len(P) is valid, including that len(P) $\geq b$; Input:

initialization vector IV;

key K.

ciphertext C, such that len(C)=len(P). Output:

Steps:

Let *n* be the smallest integer such that $n \cdot b \ge \text{len}(P)$, let $d = \text{len}(P) \cdot (n-1) \cdot b$, and let P_1 , 1. $P_2, \ldots, P_{n-1}, P_n^*$ be the unique sequence of bit strings such that:

 $P = P_1 || P_2 || \dots || P_{n-1} || P_n^*$; and

b) $P_1, P_2, ...$ and P_{n-1} are complete blocks. Consequently, $len(P_n^*)=d$, and $1 \le d \le b$, so that P_n^* is either a complete block or a nonempty partial block.

- If d=b, i.e., P_n^* is a complete block, then 2.
 - apply CBC encryption with initialization vector IV and key K to the plaintext $(P_1, P_2, ..., P_{n-1}, P_n^*)$ to produce $(C_1, C_2, ..., C_{n-1}, C_n)$;
 - return $C_1 \parallel C_2 \parallel \dots \parallel C_{n-1} \parallel C_n$. STOP.

If d < b, i.e., P_n^* is a partial block, go to Step 3.

- 3. Let PAD be the bit string consisting of b-d '0' bits, and let $P_n = P_n^* || PAD$.
- Apply CBC encryption to the plaintext $(P_1, P_2, \dots P_{n-1}, P_n)$ with initialization 4. vector IV and key K to produce $(C_1, C_2, \dots C_{n-1}, C_n)$.
- Let $C_{n-1}^* = MSB_d(C_{n-1})$. 5.
- Return $C_1 || C_2 || \dots || C_{n-2} || C_{n-1}^* || C_n$. 6.

Diagram: Figure 1 below illustrates the CBC-CS1-Encrypt algorithm for the case that The bolded rectangles contain the inputs and outputs. The dotted rectangles provide alternate representations of two blocks in order to illustrate the role of the "stolen" ciphertext.

In particular, the string of the b-d rightmost bits of C_{n-1} , denoted C_{n-1}^{**} , becomes the padding for the input block to the final invocation of the block cipher. The ciphertext that is returned in Step 6 above omits C_{n-1}^{**} , because it can be recovered from C_n during decryption.

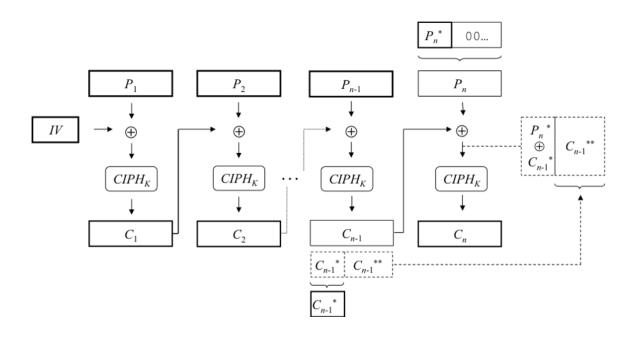


Figure 1: CBC-CS1-Encrypt

Algorithm: CBC-CS1-Decrypt

Input: ciphertext C, such that len(C) is valid, including that len $(C) \ge b$;

initialization vector *IV*;

key K.

Output: plaintext P, such that len(P) = len(C).

Steps:

- 1. Let *n* be the smallest integer such that $n \cdot b \ge \text{len}(C)$, let $d = \text{len}(C) \cdot (n-1) \cdot b$, and let C_1 , $C_2, \ldots, C_{n-2}, C_{n-1}^*$, C_n be the unique sequence of bit strings such that
 - a) $C=C_1||C_2||...||C_{n-2}||C_{n-1}^*||C_n;$
 - b) C_n is a complete block; and
 - c) If n > 2, then $C_{1,...,}C_{n-2}$, are complete blocks.

Consequently, $len(C_{n-1}^*)=d$, and $l \le d \le b$, so that C_{n-1}^* is either a complete block or a nonempty partial block.

- 2. If d=b, i.e., C_{n-1}^* is a complete block, then
 - a) apply CBC decryption to $(C_1, C_2, ..., C_{n-2}, C_{n-1}^*, C_n)$ with initialization vector IV and key K to produce $(P_1, P_2, ..., P_{n-1}, P_n)$;
 - b) return $P_1||P_2||...||P_{n-1}||P_n$. STOP.

If d < b, i.e., C_{n-1}^* is a partial block, then go to Step 3.

3. Let $Z^* = MSB_d(CIPH^{-1}_K(C_n))$, and $Z^{**} = LSB_{b-d}(CIPH^{-1}_K(C_n))$.

- 4. Let $C_{n-1}=C_{n-1}^*||Z^{**}|$.
- 5. Apply CBC decryption to $(C_1, C_2, ..., C_{n-1})$ with initialization vector IV and key K to produce $(P_1, P_2, ..., P_{n-1})$.
- 6. Let $P_n^* = C_{n-1}^* \oplus Z^*$.
- 7. Return $P_1||P_2||...||P_{n-1}||P_n^*$.

Diagram:

Figure 2 below illustrates the CBC-CS1-Decrypt algorithm for the case that d < b. As in the previous diagram, the bolded rectangles contain the inputs and outputs.

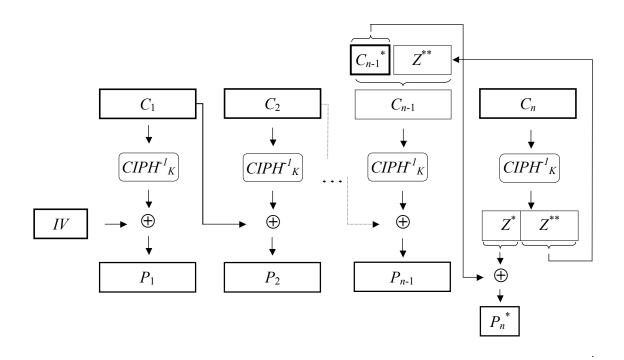


Figure 2: CBC-CS1-Decrypt

3 Specification of CBC-CS2

Algorithm: CBC-CS2-Encrypt

Input: plaintext P, such that len(P) is valid, including that len $(P) \ge b$;

initialization vector *IV*;

key K.

Output: ciphertext C, such that len(C) = len(P).

Steps:

- 1. Let n be the smallest integer such that $n \cdot b \ge \text{len}(P)$, let $d = \text{len}(P) \cdot (n-1) \cdot b$, and let P_1 , $P_2, \ldots, P_{n-1}, P_n^*$ be the unique sequence of bit strings such that:
 - $P=P_1||P_2||...||P_{n-1}||P_n^*$; and

b) P_1, P_2, \dots and P_{n-1} are complete blocks. Consequently, $len(P_n^*)=d$, and $1 \le d \le b$, so that P_n^* is either a complete block or a nonempty partial block.

- If d=b, i.e., P_n^* is a complete block, then 2.
 - apply CBC encryption with initialization vector IV and key K to the plaintext $(P_1, P_2, ..., P_{n-1}, P_n^*)$ to produce $(C_1, C_2, ..., C_{n-1}, C_n)$;
 - return $C_1 ||C_2|| \dots C_{n-1} ||C_n|$. STOP.

If d < b, i.e., P_n^* is a partial block, go to Step 3.

- Let PAD be the bit string consisting of b-d '0' bits, and let $P_n = P_n^* \parallel PAD$. 3.
- Apply CBC encryption to the plaintext $(P_1, P_2, \dots P_{n-1}, P_n)$ with initialization 4. vector IV and key K to produce $(C_1, C_2, \dots C_{n-1}, C_n)$.
- Let $C_{n-1}^* = MSB_d(C_{n-1})$. 5.
- Return $C_1 || C_2 || \dots || C_{n-2} || C_n || C_{n-1}^*$. 6.

Note that the output in Step 6 of CBC-CS2-Encrypt is almost identical to the output in Step 6 of CBC-CS1-Encrypt. The only difference is the ordering of the final b+d bits; in particular, C_n precedes C_{n-1}^* instead of following it.

Algorithm: CBC-CS2-Decrypt

ciphertext C, such that len(C) is valid, including that len(C) $\geq b$; Input:

initialization vector *IV*;

key K.

Output: plaintext P, such that len(P)=len(C).

Steps:

- 1. Let n be the smallest integer such that $n \cdot b \ge \text{len}(C)$, let $d = \text{len}(C) \cdot (n-1) \cdot b$, and let C_1 , $C_2, \ldots, C_{n-2}, C_{n-1}, C_n^*$ be the unique sequence of bit strings such that
 - $C=C_1||C_2||...||C_{n-2}||C_{n-1}||C_n^*;$
 - C_{n-1} is a complete block; and b)
 - If n > 2, then C_1, \ldots, C_{n-2} , are complete blocks.

Consequently, $len(C_n^*)=d$, and $l \le d \le b$, so that C_n^* is either a complete block or a nonempty partial block.

- If d=b, i.e., C_n^* is a complete block, then 2.
 - apply CBC decryption to $(C_1, C_2, ..., C_{n-1}, C_n^*)$ with initialization vector IV and key K to produce $(P_1, P_2, \dots, P_{n-1}, P_n)$;
 - return $P_1||P_2||...||P_{n-1}||P_n$. STOP.

If d < b, i.e., C_n^* is a partial block, then go to Step 3.

Apply Steps 3-6 of CBC-CS1-Decrypt to $C_1||C_2||...||C_{n-2}||C_n^*||C_{n-1}$ to return $P_1||P_2||$ 3. $||...||P_{n-1}||P_n^*$.

Note that in Step 3, C_n^* precedes C_{n-1} in order to undo the corresponding swap within the ciphertext in Step 6 of CBC-CS2-Encrypt.

Specification of CBC-CS3

Algorithm: CBC-CS3-Encrypt

plaintext P, such that len(P) is valid, including that len(P) $\geq b$; Input:

initialization vector *IV*;

key K.

Output: ciphertext C, such that len(C)=len(P).

Steps:

- 1. Let n be the smallest integer such that $n \cdot b \ge \text{len}(P)$, let $d = \text{len}(P) \cdot (n-1) \cdot b$, and let P_1 , $P_2, \ldots, P_{n-1}, P_n^*$ be the unique sequence of bit strings such that:
 - $P=P_1||P_2||...||P_{n-1}||P_n^*;$ and
 - P_1, P_2, \dots and P_{n-1} are complete blocks.

Consequently, $len(P_n^*)=d$, and $1 \le d \le b$, so that P_n^* is either a complete block or a nonempty partial block.

- If d=b, i.e., P_n^* is a complete block, then 2.
 - apply CBC encryption with initialization vector IV and key K to the plaintext $(P_1, P_2, ..., P_{n-1}, P_n^*)$ to produce $(C_1, C_2, ..., C_{n-1}, C_n)$; return $C_1 ||C_2|| ... ||C_{n-2}||C_n||C_{n-1}$. STOP.

If d < b, i.e., P_n^* is a partial block, go to Step 3.

- Let PAD be the bit string consisting of b-d '0' bits, and let $P_n = P_n^* || PAD$. 3.
- Apply CBC encryption to the plaintext $(P_1, P_2, \dots P_{n-1}, P_n)$ with initialization 4. vector IV and key K to produce $(C_1, C_2, \dots C_{n-1}, C_n)$.
- 5. Let $C_{n-1}^* = MSB_d(C_{n-1})$.
- Return $C_1||C_2||...||C_{n-2}||C_n||C_{n-1}^*$. 6.

Note that in Step 6 of CBC-CS3-Encrypt, as in CBC-CS2-Encrypt, the positions of C_{n-1}^* and C_n are swapped in comparison to Step 6 of CBC-CS1-Encrypt. For CBC-CS3-Encrypt, the analogous swap also occurs in the case that P_n^* is a complete block. In particular, within the output of Step 2 for CBC-CS3-Encrypt, C_n precedes C_{n-1} , in contrast to the output of Step 2 for CBC-CS1-Encrypt and CBC-CS2-encrypt, where C_n follows C_{n-1} .

Algorithm: CBC-CS3-Decrypt

Input: ciphertext C, such that len(C) is valid, including that len(C) $\geq b$;

initialization vector IV;

key K.

Output: plaintext P, such that len(P)=len(C).

Steps:

- 1. Let *n* be the smallest integer such that $n \cdot b \ge \text{len}(C)$, let $d = \text{len}(C) \cdot (n-1) \cdot b$, and let C_1 , $C_2, \ldots, C_{n-2}, C_{n-1}, C_n^*$ be the unique sequence of bit strings such that
 - a) $C=C_1||C_2||...||C_{n-2}||C_{n-1}||C_n^*;$
 - b) C_{n-1} is a complete block; and
 - c) If n>2, then $C_1,...,C_{n-2}$, are complete blocks.

Consequently, $len(C_n^*)=d$, and $1 \le d \le b$, so that C_n^* is either a complete block or a nonempty partial block.

2. Apply the CBC-CS1-Decrypt algorithm with initialization vector IV and key K to $C_1||C_2||...||C_{n-2}||C_n^*||C_{n-1}$ to return $P_1||P_2||...||P_{n-1}||P_n^*|$.

Note that in Step 2, C_n^* precedes C_{n-1} in order to undo the corresponding swaps within the ciphertexts in Steps 2b and 6 of CBS-CS3-Encrypt.

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